

Comparison of Design Forces for Metro Rail Structures

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Abstract—This paper presents a comparative study of calculation of design forces using various codes for design of metro rail structures. Design forces were calculated for superstructure and substructure of metro rail bridges using Indian and other countries codes and a comparative study has been done between them. Structures were modeled using CSI-bridge software with the thin shell and beam elements and linear finite element analysis was performed to calculate the responses. From the study, it was found that design forces calculated using different code differ widely.

Keywords: Metro Rail Structures, Finite Element Analysis.

1. INTRODUCTION

Metro bridges have two major elements: pier and prestressed box girder or beams. In almost all big cities of India metro construction work is going on but still at present nationwide guidelines are not available for the design of metro rail structure. Each metro organization in India has their own design specifications based on Indian Road Congress (IRC) or Indian Railway Standard (IRS) guidelines. The main objective of this study is to compare the design forces calculated for superstructure and substructures of metro rail bridges using IRC, IRS, Euro-code, California high-speed rail authority guidelines and other.

2. METHODOLOGY

For the study simply supported prestressed I (span 25m) and Box girder (span 40m) metro bridge were considered. Analysis of substructure and superstructure were carried out for all the static and dynamic (wind and seismic) loads as per various code and then a comparative study has been done between design forces.

2.1 Mathematical Modeling of Bridges

Cross section details of simply supported 25 m span prestressed I-girder and 40 m span Box-girder bridge are shown in Fig. 1 and Fig. 2 respectively. In I-girder bridge 5 equally spaced cross girder of thickness 0.5 m and depth 1.5 m were provided and in Box-girder three diaphragms (at support and mid-span) of thickness 1 m were provided. Mathematical

modeling of both the structures were done in CSI-Bridge 2015 software. FEM model of I and Box girder bridge are shown in Fig. 3 and Fig. 4. Before modeling minimum sizes of each section elements were checked as per IRS-Concrete Bridge Code (CBC) [1]. For both the type of bridges M45 grade of concrete and Fe 415 grade steel were used. For post-tensioning, prestressing steel conforming to class 2 low relaxation uncoated stress relieved strands were used. Cable profiles were assumed to be parabolic.

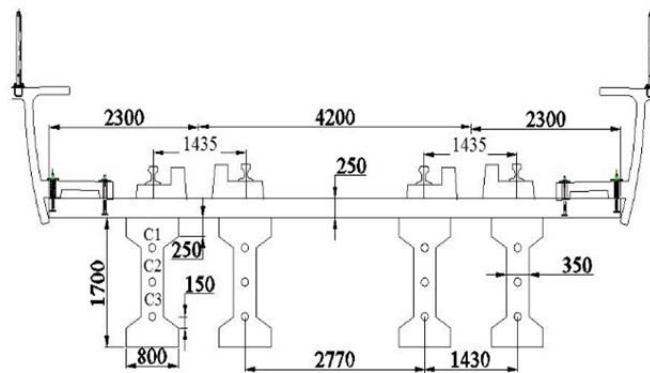


Fig. 1: Cross section of prestressed I-girder.

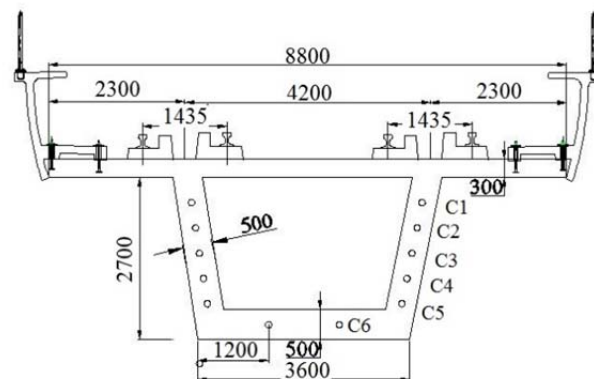


Fig. 2: Cross section of prestressed Box-girder.

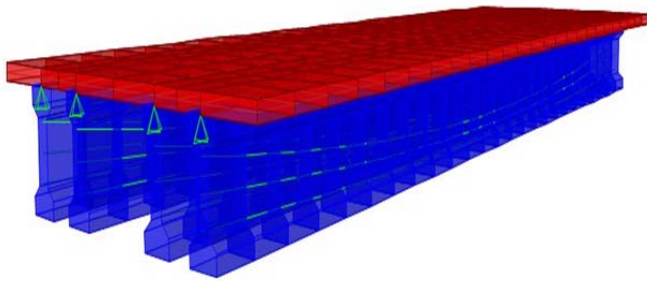


Fig. 3: Mathematical model of I-girder.

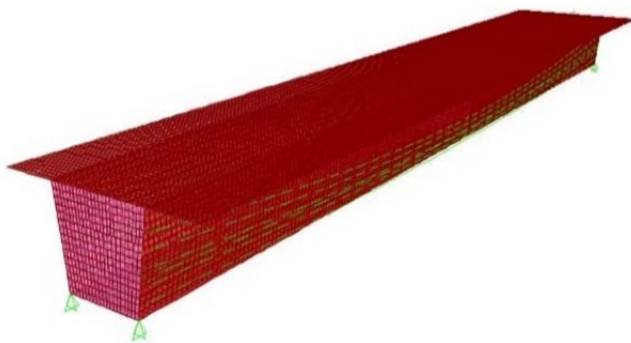


Fig. 4: Mathematical model of Box-girder.

2.2 Loading Specifications

Loading specification as per the various codes for all the static and dynamic (wind and seismic) loads are described below.

Both the Nagpur metro rail corporation Limited (NMRCL) design basis report (DBR) [2] and Hyderabad metro rail limited (HMRL) DBR [3] specify IRS Bridge Rules [4] for calculation of impact factor, longitudinal force, nosing force, force on parapet and footpath live load.

2.2.1 Super Imposed Dead Load (SIDL). SIDL is divided into two parts i.e. SIDL variable and SIDL fixed. Only parapet load comes under the fixed. SIDL load in kN/m is given in Table 1.

Table 1: SIDL for metro bridge in kN/m.

| Item | Load kN/m | Item | Load kN/m |
|--------------------------|-----------|--------------------|-----------|
| Rail + Pad | 3 | Miscellaneous | 4 |
| Cable + trays | 0.8 | Cable trays | 0.1 |
| Plinth | 28 | Hand rails | 0.8 |
| Light wt. drainage conc. | 2.4 | Cable duct cover | 2 |
| Cables through cell | 7.4 | Parapet (SIDL Fix) | 32.6 |

2.2.2 Live Load. The live load considered as per NMRCL DBR, successive cars in a train is 6 with the length of each car is 21.8 m. Each car consists four axles and load of each axle is same i.e. 160 kN as shown in Fig. 5. To calculate maximum response moving load analysis were performed in CSI-bridge for both single and double track loadings. Impact factor for I and Box girder metro bridge was calculated as per IRS: Bridge rule, EN 1991-2 [5] and California high speed rail authority [6] which is given in Table 2.

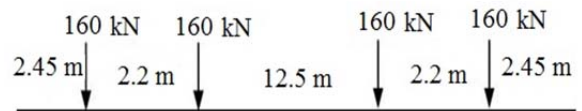


Fig. 5: Standard axle distances of Nagpur metro train.

Table 2: Impact factor for both the Bridges.

| Code | Formula | CDA I-Girder | CDA Box-Girder |
|--------------------------------------|---|--------------|----------------|
| IRS Bridge Rules | $1 + (0.15 + \frac{8}{6+L}) \geq 1.2$ | 1.4 | 1.32 |
| EN1991-2 | $\frac{2.16}{\sqrt{L}-0.2} + 0.73 \geq 1$ | 1.18 | 1.08 |
| California high speed rail authority | $I = \frac{225}{\sqrt{L}} \%$ (12 to 38.7 m) I= 20% > 39m | 1.24 | 1.2 |

2.2.3 Longitudinal Forces. Traction and braking forces were calculated for various codes which are given in Table 3, in which L' is live load on the deck

Table 3: Comparison of longitudinal force.

| Code | Traction load | Braking load |
|--------------------------------------|---------------|--------------|
| IRS: Bridge Rules | 0.2L' | 0.18L' |
| EN1991-2 | 0.25L' | 0.25L' |
| California high speed rail authority | 0.25L | 0.25L |

2.2.4 Nosing force, force on parapet and footpath live load. Nosing force, force on parapet and footpath live load are compared in Table 4 for various codes.

Table 4: Comparison of other forces.

| Code | Nosing Force (kN) | Force on parapet (kN/m) | Footpath live load (kN/m ²) |
|--------------------------------------|-------------------|-------------------------|---|
| IRS: Bridge Rules | 100 | 1.5 | 4.9 |
| EN1991-2 | 100 | 1.5 | 4 |
| California high speed rail authority | 98 | 1.5 | 4.8 |

2.2.5. Wind Load and Seismic Force. The wind and seismic forces were calculated as per the codal provisions of various codes which are given in Table 5. NMRCL suggests, for calculation of the wind and seismic forces IRS Bridge rules and RDSO guidelines for seismic design of railway bridges [7] shall be used. As per HMRL DBR both the dynamic forces to be calculated using IRC: 6 [8].

Table 5: Guidelines for calculation of the wind and seismic force.

| Load | Seismic Force | Wind Force |
|--------------------------------------|---------------------------------|---|
| IRS guidelines | IRS-Bridge rules clause 2.12 | IRS-Bridge Rules, clause 2.11 |
| IRC: 6 | IRC: 6 clause 209 | IRC: 6, clause 218 |
| Euro-code | EN 1998-1 [9] EN 1998-2 [10] | EN 1991-1-4 [11] |
| California high speed rail authority | AASHTO LRFD [12] Clause 3.10 | AASHTO LRFD With Caltrans Amendment Clause 3.8 |

3. ANALYSIS OF SUPER-STRUCTURE

Analysis of superstructure for both I and Box girder was carried out for DL, SIDL, prestressing load and live load. Variation of moment and shear force along the span for external and internal I-girder and Box girder are given in Table 7.

Table 7: Variation of moment (kNm) and shear force (kN) along span.

| S.F. kN and B.M kNm | Exterior I-Girder | | Interior I-Girder | | Box girder | |
|---------------------|-------------------|----------|-------------------|----------|------------|----------|
| | Support | Mid span | Support | Mid span | Support | Mid span |
| Dead Load | | | | | | |
| B.M | 0 | 3228 | 0 | 3155 | 0 | 35014 |
| S.F. | 474 | 0 | 424 | 0 | 3466 | 0 |
| SIDL Fix | | | | | | |
| B.M | 0 | 773 | 0 | 497 | 0 | 6520 |
| S.F. | 231 | 0 | 35 | 0 | 636 | 0 |
| SIDL Variable | | | | | | |
| B.M | 0 | 1187 | 0 | 1051 | 0 | 11570 |
| S.F. | 229 | 0 | 115 | 0 | 1128 | 0 |
| Live Load | | | | | | |
| B.M | 0 | 1870 | 0 | 1724 | 0 | 14323 |
| S.F. | 392 | 130 | 279 | 108 | 1801 | 590 |

For the calculated moments required prestressing, the location of tendons were calculated. Details of prestressing cables for both I and Box girder bridges are shown in Table 8.

Table 8: Details of prestressing cable profile for I and Box girder.

| Cable | Type | Position from Bottom at Support (mm) | Position from Bottom at Mid-span (mm) |
|------------|-------|--------------------------------------|---------------------------------------|
| Box-Girder | | | |
| C1 | 19K15 | 2280 | 1020 |
| C2 | 19K15 | 1860 | 800 |
| C3 | 19K15 | 1440 | 580 |
| C4 | 19K15 | 1020 | 360 |
| C5 | 19K15 | 600 | 140 |
| C6 | 19K15 | 250 | 140 |
| I-Girder | | | |
| C1 | 19K15 | 1300 | 500 |
| C2 | 12K15 | 850 | 350 |
| C3 | 19K15 | 400 | 150 |

All immediate and long-term prestressing losses were calculated as per IRS: CBC clause 16.8 and then max tensile and compressive stresses check at transfer and service stage were done. It was found that total prestressing losses for I-girder is 20.6% and for box girder is 21.4%. Stress check for both the bridges is given in Table 9.

Table 9: Compression and tensile stresses check at transfer and service stage.

| Stresses at top and bottom | Exterior I girder | Box girder |
|---|-------------------|------------|
| Max/Min stresses at transfer stage (MPa) | | |
| $(P/A) - (P \times e / Y_t) + (M(DL+SIDL) / Z_t)$ | 9.47 | 6.87 |
| $< 0.5f_{ci}$ or $0.4f_{ck}$ (18 MPa) | Safe | Safe |
| $(P/A) + (P \times e / Y_b) - (M(DL+SIDL) / Z_b)$ | 4.13 | 3.06 |
| > 0 (no tension) | Safe | Safe |
| Max/Min stresses at service stage (MPa) | | |
| $(P/A) - (P_e / Y_t) + (M(DL+SIDL+LL) / Z_t)$ | 11.62 | 9.07 |
| $< 0.4f_{ck}$ (18 MPa) | Safe | Safe |
| $(P/A) + (P_e / Y_b) - (M(DL+SIDL+LL) / Z_b)$ | 0.42 | 0.11 |
| > 0 (no tension) | Safe | Safe |

4. COMPARISON OF DESIGN FORCES FOR SUPER-STRUCTURE

For this study, following load combination are used to get design moment and shear force.

- i. IRS: CBC and NMRCL DBR Load comb. 1
 $1.4DL + 2SIDL_{(fix + variable)} + 2Live$ load
- ii. HMRL DBR Load comb.1
 $1.25DL + 2SIDL_{(variable)} + 1.25SIDL_{(fix)} + 1.75LL$
- iii. EN 1990 [13] Load Comb. 1
 $1.35DL + 1.5SIDL_{(variable)} + 1.35SIDL_{(fix)} + 1.45LL$

- iv. California high speed rail authority Load comb.1 (Strength 1 Basic load combination)

$$1.25DL + 1.5SIDL_{(variable)} + 1.25SIDL_{(fix)} + 1.75LL$$

Comparison of maximum design moment calculated using Indian and other countries codes for external and internal girder of I-girder bridge are shown in Fig. 6 and Fig. 7 and for Box-girder shown in Fig. 8.

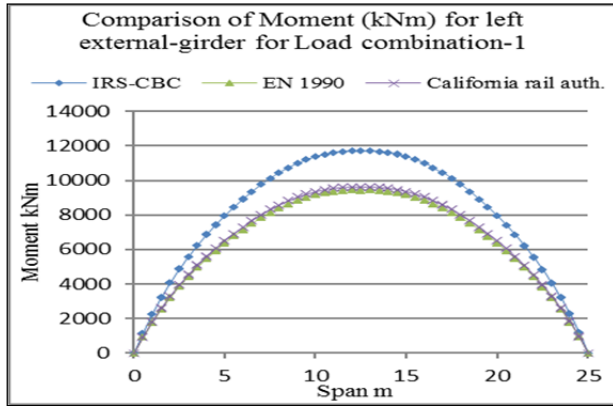


Fig. 6: Comparison of Moment (kNm) for left external girder for load combination -1

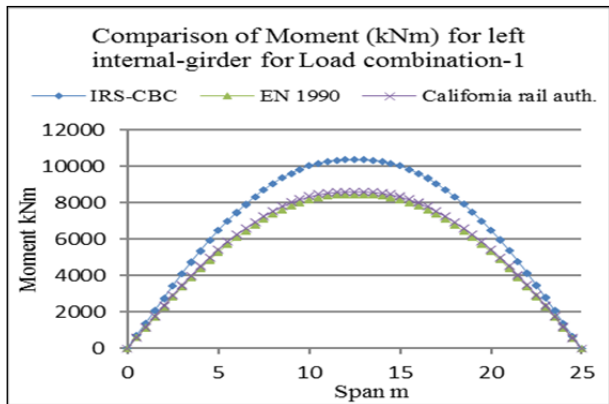


Fig. 7: Comparison of Moment (kNm) for left internal girder for load combination -1

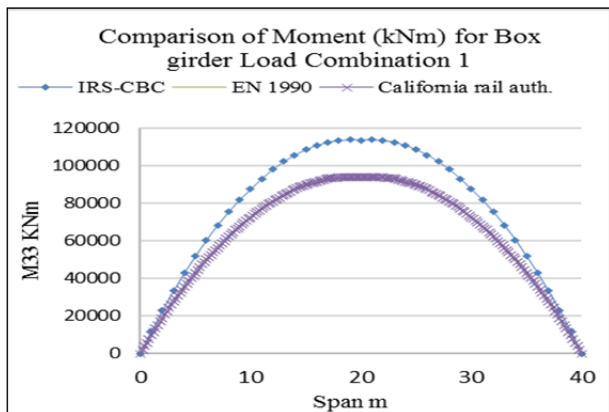


Fig. 8: Comparison of Moment (kNm) for Box-girder for load combination -1

Comparison of maximum shear force calculated using Indian and other countries codes for I-girder and Box-girder bridge are shown in Table 10.

Table 10: Comparison of shear force for load comb.-1

| EN 1990 | | IRS CBC | | California high rail authority | |
|---------------------------------------|----------|---------|----------|--------------------------------|----------|
| Span (m) | | | | | |
| Support | Mid-span | Support | Mid-span | Support | Mid span |
| Shear force at Exterior I-Girder (kN) | | | | | |
| 1863 | 188 | 2369 | 263 | 1910 | 227 |
| Shear force at Internal I-Girder (kN) | | | | | |
| 1197 | 157 | 1311 | 214 | 1234 | 189 |
| Shear force Box Girder (kN) | | | | | |
| 9841 | 856 | 11982 | 1319 | 9971 | 1032 |

From Fig. 7-9 and Table 10, it can be seen that design moment and shear force calculated as per IRS: CBC are more compared to other codes. Responses calculated as per EN 1990 are approximately equal to calculated by California guidelines. Comparing maximum moment and shear force it is observed that inner girder of I-girder bridge gives lower result than the outer girder.

5. ANALYSIS OF SUB-STRUCTURE

Analysis of substructure was done for the simply supported box girder bridge. Horizontal and vertical reactions were calculated on the pier due all static and dynamic loads (wind and seismic). General elevation diagram of Box girder bridge is shown in Fig. 9. The height of solid parapet is 1.5 m and height of train considered is 3.9 m. Sectional and material properties of the column are given in Table 11.

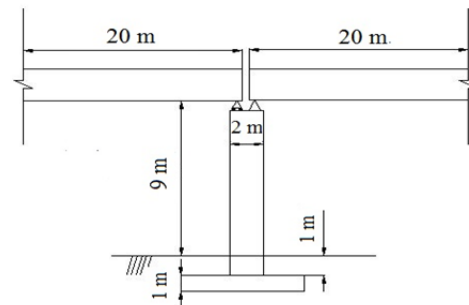


Fig. 9: Elevation Box-girder bridge

Table 11: Material and sectional properties of the pier.

| Properties | Value | Properties | Value |
|------------|-------|----------------------|--------|
| Fck (MPa) | M40 | Height (m) | 10 |
| Dia. (m) | 2 | I (mm ⁴) | 0.785 |
| K (kN/m) | 74510 | Location | Nagpur |

6. COMPARISON OF DESIGN FORCES FOR SUB-STRUCTURE

Vertical and horizontal reactions on top of the pier due all the static and dynamic (wind and seismic) loads were calculated. Horizontal and vertical reaction due to DL, SIDL, live load are given in Table 12, where H_L and H_T are the horizontal force in the longitudinal and transverse directions, Z_L and Z_T are lever arm from bottom of the footing in the longitudinal and transverse directions.

Table 12: Reactions on the pier due to Static load.

| Load Cases | Forces | | |
|----------------------|--------|-------|--------|
| | V (kN) | HL kN | ZL (m) |
| DL | 6930 | - | - |
| SIDL Fix | 1304 | - | - |
| SIDLVar | 2296 | - | - |
| Live Load | 2688 | - | - |
| Braking and traction | 44.7 | 426 | 11 |

6.1 Comparison of Reactions Due to Seismic Force

Base shear due to seismic force were calculated for the pier as per IRC: 6, IRS- Bridge rules and RDSO guidelines for seismic design of railway bridges for all the three type of soils. Comparative study for base shear is shown in Table 13.

Table 13: Comparison of base shear.

| Load Cases | Base shear and lever arm | | | |
|---|--------------------------|--------|-------|--------|
| | HL (kN) | ZL (m) | HT kN | ZT (m) |
| Seismic force as per IRS-Bridge Rules For $I = 1.5$ | | | | |
| Hard soil | 355 | 12.72 | 334 | 11 |
| Medium soil | 426 | 12.72 | 402 | 11 |
| Soft Soil | 532 | 12.72 | 502 | 11 |
| As per RDSO guidelines ($I = 1.5$ and $R = 4$) | | | | |
| Hard soil | 285 | 12.72 | 269 | 11 |
| Medium soil | 388 | 12.72 | 366 | 11 |
| Soft Soil | 476 | 12.72 | 450 | 11 |
| As per IRC: 6 ($I = 1.5$ and $R = 4$) | | | | |
| Hard soil | 277 | 12.72 | 269 | 11 |
| Medium soil | 377 | 12.72 | 366 | 11 |
| Soft Soil | 463 | 12.72 | 450 | 11 |

From Table 13 it is seen that for the particular case base shear calculated using IRS: Bridge Rule code is higher as compared to other Indian guidelines. Base shear calculated as per RDSO guidelines is same in the longitudinal direction and more in the transverse direction as compared to IRC: 6. It may be because as per IRC: 6, 20% live load is considered in transverse direction and as per RDSO guidelines 50% live load is considered.

6.2 Comparison of Reactions Due to Wind Force

Reactions due to wind force were calculated on the pier as per Indian and other countries codes and a comparative study has been done between them which is shown in Table 14.

Table 14: Comparison of wind forces on top of the pier

| Load Cases | Reaction due to wind forces | | | |
|---|-----------------------------|------|-------|-------|
| | HL kN | ZL m | HT kN | ZT m |
| Wind force as per IRS Bridge Rules | | | | |
| Unloaded deck | 66 | 11 | 265 | 13.25 |
| Loaded deck | 71 | 11 | 285 | 14.45 |
| Pier | - | - | 15 | 6.5 |
| Wind force as per IRC: 6 | | | | |
| unloaded deck | 123 | 11 | 492 | 13.25 |
| Loaded deck | 175 | 11 | 702 | 14.05 |
| pier | - | - | 18 | 6.5 |
| Wind forces as per EN: 1991-1.4 | | | | |
| Unloaded deck | 105 | 11 | 421 | 13.25 |
| Loaded deck | 160 | 11 | 640 | 14.45 |
| Pier | - | - | 9.2 | 6.5 |
| Wind forces as per California high speed rail auth. | | | | |
| Unloaded deck | 114 | 11 | 457 | 13.25 |
| Loaded deck | 169 | 11 | 685 | 14.45 |
| Pier | - | - | 14 | 6.5 |

From Table 14 it is observed that Wind forces calculated for superstructure using IRS Bridge Rule are less compared to other codes. It may be because pressure coefficient method is used in IRS Bridge rules code where as in other codes gust factor method is used. Wind forces calculated as per IRC: 6, EN: 1991-1.4 and California high speed rail authority are comparable with each other.

7. CONCLUSION

The following are broad conclusions.

1. IRS: CBC suggests higher partial safety factors for dead load, SIDL and live load in load combinations. Therefore, moment, shear force calculated as per IRS: CBC at superstructure are larger as compared to Euro-code and California high speed rail authority guidelines.
2. Seismic forces calculated on the pier as per RDSO guidelines for seismic design of railway bridges, are same in the longitudinal direction and more in the transverse direction as compared to IRC: 6.
3. Wind forces calculated at superstructure using IRS-Bridge rules is less as compared to other guidelines.

This paper shows that various codes for metro bridges give different design forces. Hence there is a need of nationwide guidelines for the design of metro rail structures.

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